

Logo interpreter

```
In[12]= consumeToSpace[s_] := With[{p = StringPosition[s, " "]},
  If[p === {}, {s, ""},
    {StringTake[s, 1 ;; p[[1, 1]] - 1], StringTake[s, p[[1, 1]] + 1 ;;]}]
]

In[13]= tokenize[s_] := First@FixedPoint[With[{ans = consumeToSpace[#[[2]]]},
  {If[ans[[1]] != "", Join[#[[1]], {ans[[1]]}], #[[1]], ans[[2]]}] &, {{}, s]}

In[14]= peelOneInstruction[] = {};
peelOneInstruction[{}] = {};
peelOneInstruction[s_List] :=
  Switch[First@s,
    "fd", {MoveForward@FromDigits[s[[2]]], s[[3 ;;]]},
    "bk", {MoveBackward@FromDigits[s[[2]]], s[[3 ;;]]},
    "lt", {LeftTurn@FromDigits[s[[2]]], s[[3 ;;]]},
    "rt", {RightTurn@FromDigits[s[[2]]], s[[3 ;;]]},
    "setbackground", {SetBackground[FromDigits[s[[2]]]], s[[3 ;;]]},
    "pd", {PenDown, Rest@s},
    "pu", {PenUp, Rest@s},
    "cs", {ClearScreen, Rest@s},
    "set", {SetColour[ToExpression[s[[2]]], s[[3 ;;]]}
  ]

In[17]= instructions[s_] :=
  First@FixedPoint[If[#[[2]] === {}, #, With[{a = peelOneInstruction[#[[2]]]},
    {Join[#[[1]], {a[[1]]}], a[[2]]}] &, {{}, tokenize@s]}

In[18]= emptyState = {Down, 90°, {0, 0}, {}, Black};

In[19]= act[ClearScreen, state_] := {state[[1]], state[[2]], state[[3]], {}, state[[5]]}
act[LeftTurn[x_], state_] :=
  {state[[1]], state[[2]] + x°, state[[3]], state[[4]], state[[5]]}
act[RightTurn[x_], state_] :=
  {state[[1]], state[[2]] - x°, state[[3]], state[[4]], state[[5]]}
act[MoveForward[x_], state_] :=
  With[{newEnd = {x Cos[state[[2]]], x Sin[state[[2]]]} + state[[3]]},
    {state[[1]], state[[2]], newEnd,
      Join[state[[4]], {If[state[[1]] === Down, Opacity[1], Opacity[0]],
        state[[5]], Line@{state[[3]], newEnd}}}, state[[5]]}]
act[MoveBackward[x_], state_] := act[MoveForward[-x], state]
act[PenDown, state_] := {Down, state[[2]], state[[3]], state[[4]], state[[5]]}
act[PenUp, state_] := {Up, state[[2]], state[[3]], state[[4]], state[[5]]}
act[SetColour[col_], state_] :=
  {state[[1]], state[[2]], state[[3]], state[[4]], col}
act[SetBackground[x_], state_] := state (*TODO this may need to change *)
```

```
In[28]:= evaluate[state_, instr_List] := First@FixedPoint[
  If[#[[2]] == {}, #, {act#[[2, 1]], #[[1]], Rest#[[2]]}] &, {state, instr}]
```

Specific property we know holds of the program we are given: it stays within 10 units vertically of its starting point.

```
In[29]:= isOk[state_] :=
  AllTrue[First/@First/@state[[4]][[3 ;; -1 ;; 3]], Abs#[[2]] ≤ 10 &]
```

```
In[30]:= display[state_] :=
  Graphics[Join[state[[4]], {Blue, Disk[state[[3]], 1], Red, Arrow[{state[[3]],
    {state[[3, 1]] + Cos[state[[2]]], state[[3, 2]] + Sin[state[[2]]}}]}],
  PlotRange → {{-100, 100}, {-10, 10}}, Background → Black]
display[None] = None;
```

```
In[32]:= allRaw = {
  "cs setbackground 0 set Blue
    pd rt 30 fd 10 bk 10 lt 120 fd 10 lt 60 pu fd 10",
  "bk 10 rt 60 fd 10 lt 120 fd 20 rt 120 pu fd 10 pd lt 120 fd 10 rt 60",
  "fd 10 pd rt 60 fd 20 set Cyan
    lt 120 fd 20 rt 60 pu fd 20 pd rt 120 fd 10 bk 10",
  "fd 10 pu fd 10 pd fd 10 rt 60 fd 10 rt 120 fd 10
    rt 60 fd 10 rt 120 pu fd 20",
  "lt 60 fd 10 pu bk 20 set Pink pd fd 10 rt 60 pu fd
    20 pd lt 60 fd 10 rt 60 pu",
  "pd bk 10 lt 60 pu fd 20 pd rt 60 fd 10 lt 60 pu bk
    10 pd rt 60 bk 10 fd 10 set White",
  "pd fd 10 pu fd 10 pd fd 10 bk 10 lt 60 fd 10 lt 120
    pu fd 20 pd fd 10 pu bk 50",
  "pd fd 10 rt 60 pu fd 10 pd rt 60 fd 20 bk 10 lt 60
    bk 10 pu fd 20 pd fd 10",
  "pd lt 120 fd 10 pu fd 40 pd lt 120 fd 20 rt 120 pu fd 40 pd rt 60 fd 20",
  "pu fd 10 rt 60 fd 60 pd fd 10
    pu fd 40 pd rt 180 set Cyan fd 20 lt 60 pu fd 10",
  "pu fd 20 pd rt 60 fd 10 set Red fd 10 lt 120 fd 10
    lt 60 fd 10 bk 10 lt 60",
  "rt 120 pu fd 30 pd rt 120 fd 10 bk 10 lt 120 pu fd
    70 pd rt 120 set Yellow fd 10",
  "rt 60 pu fd 10 pd lt 60 fd 10 rt 60 pu fd 10 pd fd
    10 pu fd 20 pd rt 60 fd 10",
  "lt 120 pu fd 10 pd fd 10 rt 60 pu fd 30 pd rt 120 fd 20 pu lt 120 fd 40"
};
```

We know `begin` comes first, and `end` comes last; the others are `instrs`.

```
In[33]:= instrs = instructions/@allRaw[[2 ;; -2]];
begin = instructions@allRaw[[1]];
end = instructions@allRaw[[-1]];

```

```
In[36]:= doIt[soFar_] :=
  With[{output = evaluate[emptyState, Flatten@{begin, Part[instrs, soFar]}]},
    If[isOk[output], display@output, None]
  ]
```

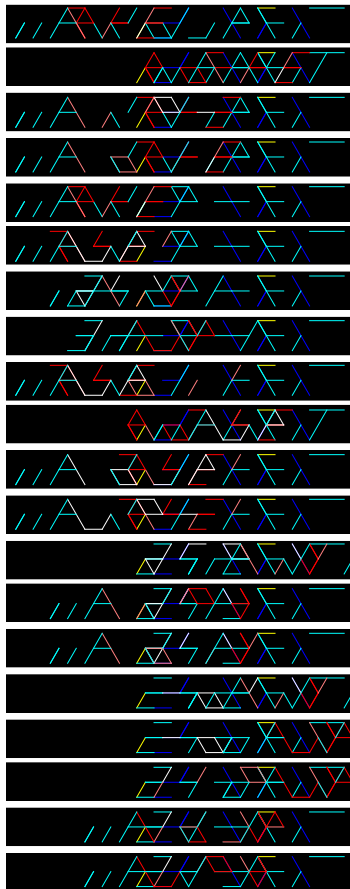
```
In[37]:= explore[x_? (Length[#] == 12 &)] = x;
explore[soFar_] := If[doIt[soFar] === None, None,
  With[{upNext =
    Select[Complement[Range[12], soFar], doIt[Join[soFar, {#}]] != None &]},
    explore[Join[soFar, {#}]] & /@ upNext
  ]
]
```

Takes a few seconds to evaluate:

```
In[39]:= allowable = Cases[explore[{}], _List? (# != {} && IntegerQ[#[[1]]] &), Infinity];
```

```
In[40]:= get[perm_] :=
  With[{output = evaluate[emptyState, Flatten@{begin, Part[instrs, perm], end}]},
    If[isOk[output], display@output, None]
  ]
```

```
In[41]:= get /@ allowable // Column
```



Out[41]=

